

## NEXT-TIME QUESTION

Most of us know that when a sheet of paper is folded in half three times, the thickness of the wad of paper is  $2 \times 2 \times 2$  or  $2^3$  or 8 times the thickness of a single sheet. The thickness of a typical sheet of thin paper is about  $7 \times 10^{-5}$  m.

If you could fold a sheet of paper in half 51 times, the height of the resulting "pile of paper" would

- a) be about 1 kilometer.
- b) reach the Moon.
- c) reach the Sun.



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**Answer:** c. reach the Sun

The "pile of paper" would reach from the Earth to the Sun!

**Calculation:** For 51 foldings we must multiply the thickness of the paper by  $2^{51} = 2.3 \times 10^{15}$ .

$$(7 \times 10^{-5} \text{ m})(2.3 \times 10^{15}) = 1.6 \times 10^{11} \text{ m.}$$

**Approximation:** Every ten doublings multiplies the thickness by a factor of  $2^{10} = 1024 \sim 10^3$ . Fifty doublings will multiply the thickness by  $2^{50} = (2^{10})^5 = (10^3)^5 = 10^{15}$ .

Fifty-one doublings multiplies the thickness by a factor of approximately  $2 \times 10^{15}$ .

When this is multiplied by the thickness of one sheet the resulting thickness of the pile of paper is  $1.4 \times 10^{11}$  m. (The distance from the Earth to the Sun is  $1.5 \times 10^{11}$  m.)

**Question:** If the original sheet of paper had an area of  $600 \text{ cm}^2$  (roughly the area of a sheet of notebook paper) and if the resulting pile of paper was a square in cross section, what would be the width of the pile of paper?

**Answer:** The volume of the original sheet is  $(6 \times 10^{-2} \text{ m}^2)(7 \times 10^{-5} \text{ m}) = 4.2 \times 10^{-6} \text{ m}^3$ .

If we assume that the volume is conserved in this redistribution of paper, then the cross-section area of a column reaching the Sun is  $4.2 \times 10^{-6} \text{ m}^3 / 1.6 \times 10^{11} \text{ m}$  or  $2.6 \times 10^{-17} \text{ m}^2$ . The edge of a square of this area is  $5.1 \times 10^{-9} \text{ m}$ . This is roughly 50 times the diameter of the hydrogen atom.

